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FEB 77 C A MORRISON, D E WORTMAN  
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20. ABSTRACT (Continue on reverse side if necessary and identify by block number) Previously reported spectra of the pentaphosphates of Nd <sup>3+</sup> and Eu <sup>3+</sup> are analyzed by diagonalizing a parametrized (C <sub>s</sub> (C <sub>1h</sub> )) Hamiltonian in free-ion bases involving the five and seven lowest J-multiplets, respectively, of each ion. By reassigning symmetries to the reported Eu levels according to predictions from scaled crystal field parameters, B <sub>km</sub> , that fit 28 Nd <sup>3+</sup> levels to		

Eu(3+)

B sub km

Nd(3+)

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7.61  $\text{cm}^{-1}$ , a fit of 10.43  $\text{cm}^{-1}$  to 46  $\text{Eu}^{3+}$  levels is obtained. Predicted  $B_{km}$  and energy levels for all the lanthanide pentaphosphates are then obtained.

B sub km

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## 1. INTRODUCTION

Interest in new materials that have potentially good laser properties has recently been focused on the rare-earth pentaphosphates.<sup>1</sup> The apparent lack of quenching between the active ions in these materials, as evidenced by the sharp lines observed even when there is 100-percent doping as in  $\text{NdP}_5\text{O}_{14}$ , leads to the obvious expectation of producing smaller laser crystals with these materials.

In this work, previously reported spectra of the pentaphosphates of Nd and Eu were analyzed by diagonalizing a parametrized  $C_s(C_{1h})$  Hamiltonian in free-ion bases involving the five and seven lowest J-multiplets, respectively, of each ion. By reassigning symmetries to the reported<sup>2</sup> Eu levels according to predictions from scaled crystal field parameters,  $B_{km}$ , that fit 28 Nd levels<sup>3</sup> to  $7.61 \text{ cm}^{-1}$ , a fit of  $10.43 \text{ cm}^{-1}$  to 46 levels of Eu was obtained. Predicted  $B_{km}$  and energy levels for all the lanthanide pentaphosphates also were obtained.

## 2. CALCULATIONS

The point group symmetry at the rare-earth ion site<sup>4,5</sup> is  $C_1$  which gives rise to the crystal field Hamiltonian

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<sup>1</sup>H. G. Danielmeyer and H. P. Weber, *IEEE J. Quantum Electron.*, **QE-8** (1972), 805.

<sup>2</sup>C. Brecher, *J. Chem. Phys.*, **61** (1974), 2297.

<sup>3</sup>M. Blatte, H. G. Danielmeyer, and R. Ulrich, *Appl. Phys.*, **1** (1973), 275.

<sup>4</sup>H. Y-P Hong, *Acta Crystallogr.*, **B30** (1974), 468.

<sup>5</sup>K.-R. Albrand, R. Attig, J. Fenner, J. P. Jeser, and D. Mootz, *Mater. Res. Bull.*, **9** (1974), 129.

$$H_x = \sum_{km} B_{km} C_{km}, \quad k = 2, 4, 6, \quad (1)$$

where  $|m| \leq k$  and  $B_{km}$  for  $m \neq 0$  may be complex. This Hamiltonian represents the lowest possible symmetry in the electrostatic potential at the rare-earth site, and it contains 26 independent  $B_{km}$ , counting real and imaginary parts of the  $B_{km}$ . In order to obtain a manageable representation for the crystal field that may be extended to predict spectra of all the lanthanide pentaphosphates, we assume the  $B_{km}$  with  $m = \pm$  odd integer to be negligible (subject to justification at a later date). The resulting Hamiltonian given by equation (1) with the added restriction

$$m = 0, \pm 2, \dots, \pm k \quad (2)$$

results in 14 independent parameters and has the appearance of  $C_s(C_{1h})$  symmetry.

This Hamiltonian was diagonalized in free-ion bases by using the lowest five and seven J-multiplets, respectively, of Nd and Eu, and the  $B_{km}$  and multiplet centroids were varied to fit reported spectra for  $NdP_5O_{14}$ <sup>3</sup> and  $EuP_5O_{14}$ .<sup>2</sup> To begin the analysis, the  $B_{km}$  of Brecher<sup>2</sup> were converted from the form  $A_k^m \langle r^k \rangle$  to the  $B_{km}$  of equation (1). These  $B_{km}$ , given in table I, line 1, were then used to calculate theoretical energy levels for the <sup>7</sup>F term of Eu. Crystal quantum numbers  $\mu = 0, 1$  were assigned to experimental energy levels according to which theoretical level each approximated. By maintaining these assignments, the  $B_{km}$  and

<sup>2</sup>C. Brecher, *J. Chem. Phys.*, **61** (1974), 2297.

<sup>3</sup>M. Blatte, H. G. Danielmeyer, and R. Ulrich, *Appl. Phys.*, **1** (1973), 275.

<sup>6</sup>A. J. Kassman, *J. Chem. Phys.*, **53** (1970), 4118.



centroids were varied to give a best fit of  $14.6 \text{ cm}^{-1}$  for 49 levels with the  $B_{km}$  of table I, line 2. These  $B_{km}$  were then scaled according to the ratios<sup>7</sup>

$$B_{km}(\text{Nd})/B_{km}(\text{Eu}) = 1.024, 1.194, 1.271; k = 2, 4, 6, \quad (3)$$

and used as starting parameters to fit the 28 levels of the  $^4I$  term and  $^4F_{3/2}$  multiplet of Nd. A fit of  $7.6 \text{ cm}^{-1}$  was obtained with the  $B_{km}$  of table I, line 4.

Since the final  $B_{km}$  for Nd differed significantly from the initial set, they were then scaled back to Eu to determine if new crystal quantum number assignments to the Eu levels would result in a better fit. By maintaining the new assignments, a second set of  $B_{km}$  given in table I, line 3, was obtained that gave a fit of  $13.2 \text{ cm}^{-1}$ , better than the  $14.6 \text{ cm}^{-1}$  resulting from Brecher's assignments, but not as good a fit as the Nd spectrum. Three experimental levels at 1928, 4952, and  $4993 \text{ cm}^{-1}$  differed by more than  $30 \text{ cm}^{-1}$  from theoretical values in the best-fit calculation for Eu. If they are ignored, the  $13.2\text{-cm}^{-1}$  fit for 49 levels is reduced to a  $10.4\text{-cm}^{-1}$  fit without any further refitting of the  $B_{km}$  to the remaining 46 levels.

Comparing the final parameters for Eu in table I, line 3, with those of Nd in line 4, it is not clear what the best way is of extending the results to all the lanthanides. There is some consistency between the parameters, however, if one compares the rotational invariants  $B_{oo}(k, N)$  for each ion where we define<sup>8</sup>

$$B_{oo}(k, N) = \left[ \sum_m |B_{km}(N)|^2 \right]^{1/2}, \quad (4)$$

<sup>7</sup>N. Karayianis, D. E. Wortman, and C. A. Morrison, *Crystal Field Parameters for Triply Ionized Lanthanides in Yttrium Orthoaluminate*, *Solid State Communications* 18 (1976), 1299.

<sup>8</sup>N. Karayianis, C. A. Morrison, and D. E. Wortman, *J. Chem. Phys.*, 64 (1976), 3890.



TABLE 1. CRYSTAL FIELD PARAMETERS,  $B_{km}$ , IN  $\text{CM}^{-1}$  FOR  $\text{NdP}_5\text{O}_{14}$  AND  $\text{EuP}_5\text{O}_{14}$

Ion	$B_{2,0}$	$B_{2,2}$	$B_{4,0}$	$B_{4,2}$		$B_{4,4}$		$B_{6,0}$		$B_{6,2}$		$B_{6,4}$		$B_{6,6}$		Multi-plets (No.)	Levels (No.)	Experi-mental levels (No.)	Energy rms deviation ( $\text{cm}^{-1}$ )
				Real	Imaginary	Real	Imaginary	Real	Imaginary	Real	Imaginary	Real	Imaginary						
$\text{Eu}^a$	-508	167	648	146	0	-847	0	195	74	0	75	0	-401	0	7	49	49	18.94	
$\text{Eu}^b$	-453	270	720	114	100	-799	49	245	97	-41	-22	-257	-424	-16	7	49	49	14.56	
$\text{Eu}^c$	-586	213	-83	751	80	111	-184	132	-118	388	81	-68	-457	-3	7	40	49	13.18	
$\text{Nd}^d$	-785	16	-219	-661	149	-621	52	291	-242	-275	249	-391	18	-176	5	28	46	10.43	
																28	28	7.61	

<sup>a</sup> Brecher's parameters with J-mixing included and centroids adjusted for best rms fit (C. Brecher, J. Chem. Phys., 61 (1974), 2297).

<sup>b</sup> Best  $B_{km}$  fitting levels with crystal quantum number assignments from calculation of line 1.

<sup>c</sup> Best  $B_{km}$  fitting levels with crystal quantum number assignments starting with  $B_{km}$  scaled from line 4.

<sup>d</sup> Best  $B_{km}$  starting with  $B_{km}$  scaled from line 2.

and  $N$  represents the configuration  $f^N$  of the particular lanthanide. Table II gives the quantities  $B_{oo}(k, 3)$  and  $B_{oo}(k, 6)$  calculated for Nd and Eu, respectively, by using their final  $B_{km}$  values from table I. These quantities tend toward lower values as  $N$  gets larger. To derive  $B_{km}$  for all the lanthanides, we defined<sup>8</sup> average constants  $\eta_{km}$  independent of  $N$  by

$$\eta_{km} = \frac{1}{2} \left[ \frac{|B_{km}(Nd)|}{B_{oo}(k, 3)} + \frac{|B_{km}(Eu)|}{B_{oo}(k, 6)} \right], \quad (5)$$

chose expressions for the  $B_{oo}(k, N)$  and phases  $\phi_{km}(N)$  linear in  $N^*$  to fit the values in tables II and I, respectively, and calculated  $B_{km}$  for all the lanthanides by

$$B_{km}(N) = \eta_{km} B_{oo}(k, N) \exp[i\phi_{km}(N)]. \quad (6)$$

The parameters given by equation (6) were reported elsewhere.<sup>8</sup> A simpler method was used here, however, to obtain the  $B_{km}$  for the lanthanides. This method consists of deriving a set of  $B_{km}$  such that

$$B_{km}(N) = B_{km}(x) + \rho_k(N)/\rho_k(x) \quad (7)$$

for  $x = Nd$  and then for  $x = Eu$ ; the  $\rho_k$  are from table II by Karayianis et al.<sup>7</sup> The resulting  $B_{km}$  were then averaged, and these parameters are given in table III.

\* $N$  is the number of equivalent 4f electrons specifying the electronic configuration for that ion.  $N = 2$  for Pr, 3 for Nd, etc.

<sup>7</sup>N. Karayianis, D. E. Wortman, and C. A. Morrison, *Crystal Field Parameters for Triply Ionized Lanthanides in Yttrium Orthoaluminate, Solid State Communications* **18** (1976), 1299.

<sup>8</sup>N. Karayianis, C. A. Morrison, and D. E. Wortman, *J. Chem. Phys.*, **64** (1976), 3890.

TABLE II. ROTATIONAL INVARIANTS  $B_{00}(k, N) = (\sum_m |B_{km}(N)|^2)^{1/2}$  FOR  $NdP_5O_{14}$  AND  $EuP_5O_{14}$

	Nd	Eu
k	$B_{00}(k, 3)^a$	$B_{00}(k, 6)^b$
2	785	659
4	1320	1114
6	920	887

<sup>a</sup>Calculated from table I, line 4.

<sup>b</sup>Calculated from table I, line 3.

Energy levels calculated by using the  $B_{km}$  of tables I and III for the lowest-lying six to eight multiplets of the lanthanide pentaphosphates are given in tables IV to XVI.

In order to make intensity calculations, some estimates of the odd-fold (odd-k) crystal field components ( $A_{km}$ ) are necessary. These can be obtained by appropriate lattice sums.<sup>9</sup> In this work, we have performed the lattice sums for  $NdP_5O_{14}$  using the x-ray data of Hong<sup>4</sup> for oxygen charges  $q_0 = -1$  and  $-2$ ; the results are given in table XVII. The one fold field,  $A_{1m}$ , is not expected to be accurate because of its slow convergence. By appropriate rotations of the coordinate system chosen for the calculation of the  $A_{km}$  of table XVII, different sets of  $A_{km}$  can be generated. Since the  $A_{km}$  are linear functions of  $q_0$ , a value of  $q_0$

can be chosen by using the relation  $B_{km} = \rho_k A_{km}$  and the  $\rho_k$  (reported in table II by Karayianis<sup>7</sup>) to obtain a best fit of calculated  $B_{km}$  to phenomenological  $B_{km}$ .

<sup>4</sup>H. Y-P Hong, *Acta Crystallogr.*, **B30** (1974), 468.

<sup>7</sup>N. Karayianis, D. E. Wortman, and C. A. Morrison, *Crystal Field Parameters for Triply Ionized Lanthanides in Yttrium Orthoaluminate*, *Solid State Communications* **18**(1976), 1299.

<sup>9</sup>N. Karayianis and C. A. Morrison, *Rare Earth Ion-Host Lattice Interactions 1. Point Charge Lattice Sum in Scheelites*, *Harry Diamond Laboratories TR-1648* (October 1973).

TABLE III. ESTIMATED CRYSTAL FIELD PARAMETERS,  $B_{km}$ , IN  $\text{CM}^{-1}$  FOR  $\text{LnP}_5\text{O}_{14}$  (SPACE GROUP  $P_{21}/C$ ) WHERE  $\text{Ln}$  IS ONE OF THE LANTHANIDES

Ion	$B_{20}$	$B_{22}$	$B_{40}$	$B_{4,2}$		$B_{4,4}$		$B_{6,0}$	$B_{6,2}$		$B_{6,4}$		$B_{6,6}$		rms $\text{cm}^{-1}$	Table No.
				Real	Imaginary	Real	Imaginary		Real	Imaginary	Real	Imaginary	Real	Imaginary		
Pr	-780	158	-164	-621	-536	-152	-474	240	-338	205	156	-312	210	-301	-	IV
Nd	-755	153	-159	-773	174	-479	40	235	-256	-290	183	-288	36	-357	9.739 <sup>a</sup>	VI
Pm	-729	148	-153	-307	698	-66	459	230	236	-295	208	-261	-139	-322	-	VII
Sm	-703	142	-147	364	636	415	160	224	324	176	228	-232	-272	-209	-	VIII
Eu	-675	137	-140	696	82	238	-353	218	-114	341	245	-202	-330	-49	b	X
Gd	-646	131	-134	457	-487	-277	-296	213	-346	-52	258	-171	-304	115	-	XI
Tb	-616	125	-127	-114	-623	-332	193	207	-9	-340	267	-139	-204	242	-	XII
Dy <sup>c</sup>	-584	118	-119	-535	-262	107	346	201	324	-66	271	-107	-59	301	-	XIII
Ho <sup>c</sup>	-551	112	-111	-494	257	337	-25	194	118	297	272	-76	92	283	-	XIV
Er <sup>c</sup>	-515	104	-103	-81	508	47	-308	188	-263	162	269	-45	211	195	-	XV
Tm <sup>c</sup>	-477	97	-94	328	334	-264	-105	181	-198	-222	263	-16	269	65	-	XVI

<sup>a</sup> Fit to data of C. Brecher, J. Chem. Phys., 61 (1974), 2297.

<sup>b</sup> Fit to data of table I, lines 1 and 2.

<sup>c</sup> These lanthanides have not been grown in the  $P_{21}/C$  space group structure.



TABLE IV. ESTIMATED CRYSTAL FIELD PARAMETERS AND ENERGY LEVELS FOR  
PrP5O14

PR IN PRP5O14. INTERPOLATED BKM FROM COMPATIBLE NO AND EU HOMES. 9/24/75.

INIT. BKM AND CENTROIDS. Q = -0.000

-779.700 = B20 159.100 = B22 -164.300 = B40 -620.700 = B42 -536.400 = B42  
240.100 = B60 -337.700 = B62 205.400 = B62 155.700 = B64 -312.400 = B64

3H 4 251.0  
3H 5 2354.0 -151.500 = B44 -474.500 = B44  
3H 6 4527.0 210.500 = B66 -300.700 = B66  
3F 2 5101.0  
3F 3 6478.0  
3F 4 6950.0  
1G 4 9923.0  
1D 2 16802.0

FREE ION	PCT PURE	ZMU	THEO.ENERGY	EXP.ENERGY
1 3H 4	99.6	2	-65.1	0.0
2 3H 4	99.3	0	-14.6	0.0
3 3H 4	99.5	0	70.4	0.0
4 3H 4	99.4	2	203.3	0.0
5 3H 4	99.5	2	243.6	0.0
6 3H 4	99.5	0	305.3	0.0
7 3H 4	99.6	2	333.9	0.0
8 3H 4	99.2	0	483.7	0.0
9 3H 4	99.5	0	523.4	0.0
10 3H 5	99.1	2	2077.1	0.0
11 3H 5	99.0	0	2085.7	0.0
12 3H 5	98.7	0	2187.9	0.0
13 3H 5	98.7	2	2238.3	0.0
14 3H 5	99.1	2	2295.7	0.0
15 3H 5	99.0	0	2387.1	0.0
16 3H 5	99.2	2	2397.7	0.0
17 3H 5	98.7	0	2407.4	0.0
18 3H 5	99.2	0	2440.9	0.0
19 3H 5	98.8	2	2598.7	0.0
20 3H 5	99.4	2	2617.1	0.0
21 3H 6	98.7	2	4177.9	0.0
22 3H 6	98.9	0	4178.3	0.0
23 3H 6	97.7	0	4310.5	0.0
24 3H 6	98.4	2	4351.9	0.0
25 3H 6	98.7	2	4416.8	0.0
26 3H 6	98.4	0	4484.4	0.0
27 3H 6	98.2	0	4515.7	0.0
28 3H 6	97.1	2	4590.2	0.0
29 3H 6	98.1	0	4617.2	0.0
30 3H 6	98.5	2	4631.3	0.0
31 3H 6	97.6	2	4667.8	0.0
32 3H 6	92.2	0	4812.9	0.0
33 3H 6	95.8	0	4823.7	0.0
34 3F 2	94.5	0	5060.7	0.0
35 3F 2	97.1	0	5070.0	0.0
36 3F 2	96.7	2	5146.3	0.0
37 3F 2	97.2	2	5172.2	0.0
38 3F 2	92.7	0	5220.3	0.0
39 3F 3	96.1	2	6402.9	0.0
40 3F 3	98.3	2	6445.1	0.0
41 3F 3	96.0	0	6474.1	0.0
42 3F 3	97.6	2	6512.6	0.0
43 3F 3	96.1	0	6514.0	0.0
44 3F 3	98.7	2	6555.9	0.0
45 3F 3	94.8	0	6570.0	0.0
46 3F 4	97.3	0	6819.3	0.0
47 3F 4	95.1	0	6866.8	0.0
48 3F 4	94.7	2	6896.4	0.0



TABLE IV. ESTIMATED CRYSTAL FIELD PARAMETERS AND ENERGY LEVELS FOR  
PrP<sub>5</sub>O<sub>14</sub> (Cont'd)

FREE ION	PCT PURE	2MU	THEO.ENERGY	EXP.ENERGY
49 3F 4	99.2	2	6929.0	0.0
50 3F 4	99.3	2	7002.0	0.0
51 3F 4	96.7	0	7029.3	0.0
52 3F 4	98.7	0	7043.4	0.0
53 3F 4	98.4	2	7072.7	0.0
54 3F 4	98.0	0	7091.4	0.0
55 1G 4	99.5	0	9647.3	0.0
56 1G 4	99.8	2	9787.5	0.0
57 1G 4	99.9	0	9790.4	0.0
58 1G 4	99.9	2	9863.4	0.0
59 1G 4	99.9	2	9950.7	0.0
60 1G 4	99.9	0	9965.6	0.0
61 1G 4	99.9	0	10080.2	0.0
62 1G 4	99.9	2	10129.5	0.0
63 1G 4	99.7	0	10157.1	0.0
64 1D 2	100.0	0	16523.0	0.0
65 1D 2	99.9	2	16742.3	0.0
66 1D 2	100.0	0	16748.8	0.0
67 1D 2	99.9	0	16961.4	0.0
68 1D 2	100.0	2	17069.0	0.0

TABLE V. ENERGY LEVELS AND PHENOMENOLOGICAL CRYSTAL FIELD PARAMETERS,  $B_{km}$ , for  $Nd^{3+}$  in  $NdP_5O_{14}$ <sup>a</sup>

ND IN ULTRA PHOS BLATTE ET AL DATA. HOME OVER NITE OF SEPT. 18, 1975.

FINAL BKM AND CENTRICIDS. 0 = 7.607

-785.211 = B20    16.203 = B22    -218.583 = B4C    -661.206 = B42    148.620 = B42  
230.619 = B60    -242.267 = B62    -274.634 = B62    248.941 = B64    -391.441 = B64

4I 9/2    182.7  
4I11/2    2055.4    -620.883 = B44    51.669 = B44  
4I13/2    4036.3    18.127 = B66    -175.697 = B66  
4I15/2    6083.5  
4F 3/2    11523.6

FREE ION	PCT PURE	2MU	THEO. ENERGY	EXP. ENERGY
1 4I 9/2	99.6	1	-8.4	0.C*
2 4I 9/2	99.4	1	86.3	82.C
3 4I 9/2	99.4	1	195.4	207.C*
4 4I 9/2	99.6	1	258.3	256.C
5 4I 9/2	99.7	1	329.3	317.C*
6 4I11/2	99.4	1	1956.6	1958.C
7 4I11/2	99.1	1	1981.3	1982.C
8 4I11/2	99.1	1	2035.1	2044.C*
9 4I11/2	99.2	1	2075.9	2062.C*
10 4I11/2	99.3	1	2104.5	2097.C
11 4I11/2	99.4	1	2166.3	2178.C*
12 4I13/2	99.5	1	3917.6	3914.C
13 4I13/2	99.2	1	3945.2	3943.C
14 4I13/2	99.1	1	3997.8	3995.0
15 4I13/2	99.6	1	4032.5	4037.C
16 4I13/2	99.1	1	4078.0	4090.C*
17 4I13/2	99.5	1	4116.9	4106.C*
18 4I13/2	99.5	1	4166.7	4171.C
19 4I15/2	99.4	1	5871.4	5872.C
20 4I15/2	99.6	1	5910.9	5912.C
21 4I15/2	99.6	1	6019.1	6011.C*
22 4I15/2	99.8	1	6065.0	6072.C
23 4I15/2	99.6	1	6094.4	6081.C*
24 4I15/2	99.8	1	6207.1	6210.C
25 4I15/2	99.9	1	6264.0	6274.C*
26 4I15/2	99.9	1	6287.8	6289.C
27 4F 3/2	100.0	1	11468.1	11473.C
28 4F 3/2	100.0	1	11587.4	11583.C

CENTRICIDS, CRYSTAL = 4043.2    FREE ION = 4043.4

<sup>a</sup>The least-rms deviation between the calculated and experimental energy levels is  $7.61 \text{ cm}^{-1}$  (M. Blatte, H. G. Danielmeyer, and R. Ulrich, Appl. Phys., 1 (1973), 275).

TABLE VI. ESTIMATED CRYSTAL FIELD PARAMETERS AND ENERGY LEVELS FOR  
NdP<sub>5</sub>O<sub>14</sub>

ND IN NdP<sub>5</sub>O<sub>14</sub>. EXTERPOLATED RKM FROM COMPATIBLE ND AND EU HOMES. 9/24/75.

INIT. RKM AND CENTROIDS. Q = -0.000

-754.900 = B20      153.000 = B22      -158.600 = B40      -772.800 = B42      174.200 = B42  
234.900 = B60      -255.500 = B62      -290.300 = B62      183.400 = B64      -288.000 = B64

4I 9/2      182.7  
4I11/2      2055.4      -474.300 = B44      40.100 = B44  
4I13/2      4036.3      36.500 = B66      -357.300 = B66  
4I15/2      6083.5

4F 3/2      11523.6

4F 5/2      12403.0

2H 9/2 2      12670.0

4F 7/2      13476.0

4S 3/2      13583.0

4F 9/2      14760.0

FREE ION	PCT PURE	2MU	THEO. ENERGY	EXP. ENERGY
1 4I 9/2	99.5	1	-4.6	0.0
2 4I 9/2	99.6	1	73.8	0.0
3 4I 9/2	99.5	1	201.0	0.0
4 4I 9/2	99.4	1	256.5	0.0
5 4I 9/2	99.7	1	326.6	0.0
6 4I11/2	99.5	1	1960.3	0.0
7 4I11/2	99.2	1	1973.2	0.0
8 4I11/2	99.1	1	2031.5	0.0
9 4I11/2	99.0	1	2083.7	0.0
10 4I11/2	99.3	1	2100.7	0.0
11 4I11/2	99.5	1	2161.8	0.0
12 4I13/2	99.4	1	3920.8	0.0
13 4I13/2	99.4	1	3942.8	0.0
14 4I13/2	99.2	1	3990.3	0.0
15 4I13/2	99.3	1	4022.3	0.0
16 4I13/2	99.1	1	4086.1	0.0
17 4I13/2	99.4	1	4112.0	0.0
18 4I13/2	99.6	1	4163.5	0.0
19 4I15/2	99.4	1	5865.5	0.0
20 4I15/2	99.5	1	5921.0	0.0
21 4I15/2	99.8	1	6016.7	0.0
22 4I15/2	99.7	1	6048.4	0.0
23 4I15/2	99.5	1	6083.3	0.0
24 4I15/2	99.8	1	6212.9	0.0
25 4I15/2	99.9	1	6255.0	0.0
26 4I15/2	99.9	1	6293.3	0.0
27 4F 3/2	98.6	1	11451.7	0.0
28 4F 3/2	98.9	1	11576.6	0.0
29 4F 5/2	97.3	1	12336.0	0.0
30 4F 5/2	94.9	1	12399.8	0.0
31 4F 5/2	96.4	1	12462.0	0.0
32 2H 9/2 2	98.3	1	12577.6	0.0
33 2H 9/2 2	96.8	1	12603.0	0.0
34 2H 9/2 2	98.5	1	12678.1	0.0
35 2H 9/2 2	98.5	1	12754.5	0.0
36 2H 9/2 2	98.9	1	12755.3	0.0
37 4F 7/2	99.0	1	13370.7	0.0
38 4F 7/2	98.6	1	13475.9	0.0
39 4F 7/2	98.7	1	13493.9	0.0
40 4S 3/2	85.5	1	13579.3	0.0
41 4F 7/2	64.9	1	13589.5	0.0
42 4S 3/2	79.5	1	13593.1	0.0

TABLE VI. ESTIMATED CRYSTAL FIELD PARAMETERS AND ENERGY LEVELS FOR  
NdP<sub>5</sub>O<sub>14</sub> (Cont'd)

FREE ION	PCT PURE	2MU	THEO.ENERGY	EXP.ENERGY
43 4F 9/2	99.6	1	14655.2	0.C
44 4F 9/2	99.6	1	14711.5	0.C
45 4F 9/2	99.3	1	14793.8	0.C
46 4F 9/2	99.8	1	14937.6	0.C
47 4F 9/2	99.8	1	14950.0	0.C



TABLE VII. ESTIMATED CRYSTAL FIELD PARAMETERS AND ENERGY LEVELS FOR  
PmP<sub>5</sub>O<sub>14</sub>

PM IN PMP5O14. EXTERPOLATED BKM FROM COMPATIBLE NO AND EU HOMES. 7/24/75.

INIT. BKM AND CENTRICDS. C = -0.000

-729.300 = B20    147.800 = B22    -152.800 = B40    -307.400 = B42    698.400 = B44  
229.500 = B60    235.800 = B62    -295.400 = B62    207.700 = B64    -261.200 = B66

51 4    233.0  
51 5    1731.0    -65.700 = B44    455.600 = B44  
51 6    3306.0    -138.800 = B66    -322.400 = B66  
51 7    4953.0  
51 8    6716.0  
5F 1    12298.0

FREE	IDN	PCT	PURE	2MU	THEO. ENERGY	EXP. ENERGY
1	51 4		99.7	0	115.9	0.0
2	51 4		99.7	2	142.6	0.0
3	51 4		99.7	0	142.9	0.0
4	51 4		99.4	2	153.7	0.0
5	51 4		99.2	0	169.5	0.0
6	51 4		98.9	2	215.2	0.0
7	51 4		99.5	0	286.9	0.0
8	51 4		98.5	0	355.3	0.0
9	51 4		98.9	2	393.1	0.0
10	51 5		99.4	2	1620.5	0.0
11	51 5		99.6	2	1633.3	0.0
12	51 5		98.9	0	1697.4	0.0
13	51 5		99.3	0	1700.9	0.0
14	51 5		99.1	2	1710.2	0.0
15	51 5		99.3	0	1721.2	0.0
16	51 5		98.5	2	1735.2	0.0
17	51 5		99.0	0	1770.2	0.0
18	51 5		98.2	2	1792.6	0.0
19	51 5		99.6	2	1809.6	0.0
20	51 5		98.2	0	1827.0	0.0
21	51 6		99.7	0	3200.2	0.0
22	51 6		99.8	0	3201.9	0.0
23	51 6		99.4	2	3254.2	0.0
24	51 6		99.5	2	3270.5	0.0
25	51 6		98.9	0	3281.8	0.0
26	51 6		99.1	2	3287.1	0.0
27	51 6		98.7	0	3305.2	0.0
28	51 6		98.8	2	3319.5	0.0
29	51 6		99.1	0	3326.2	0.0
30	51 6		99.1	0	3364.8	0.0
31	51 6		98.6	2	3366.5	0.0
32	51 6		99.4	0	3389.6	0.0
33	51 6		99.4	2	3391.1	0.0
34	51 7		99.7	2	4455.9	0.0
35	51 7		99.8	2	4456.4	0.0
36	51 7		99.3	0	4482.5	0.0
37	51 7		99.8	0	4485.6	0.0
38	51 7		99.0	2	4488.5	0.0
39	51 7		99.2	0	4491.8	0.0
40	51 7		99.4	2	4730.7	0.0
41	51 7		99.4	2	4739.7	0.0
42	51 7		98.9	0	4785.9	0.0
43	51 7		98.9	0	4792.2	0.0
44	51 7		99.1	2	5017.8	0.0
45	51 7		99.0	2	5031.3	0.0
46	51 7		99.1	0	5039.3	0.0
47	51 7		99.1	0	5051.1	0.0
48	51 7		99.1	2	5052.3	0.0
49	51 8		100.0	0	6547.6	0.0
50	51 8		100.0	2	6548.1	0.0
51	51 8		99.9	0	6586.4	0.0
52	51 8		99.9	2	6588.2	0.0
53	51 8		99.8	0	6591.1	0.0
54	51 8		99.8	2	6595.4	0.0
55	51 8		99.8	0	6670.7	0.0
56	51 8		99.8	0	6682.3	0.0
57	51 8		99.7	2	6694.4	0.0
58	51 8		99.5	2	6731.2	0.0
59	51 8		99.5	0	6751.5	0.0
60	51 8		99.7	2	6814.8	0.0



TABLE VII. ESTIMATED CRYSTAL FIELD PARAMETERS AND ENERGY LEVELS FOR  
 $\text{PmP}_{5014}$

FREE ION	PCT PURE	ZMU	THEO.ENERGY	EXP.ENERGY
61 5I 8	99.6	0	6422.5	0.0
62 5I 8	99.6	0	6431.5	0.0
63 5I 8	99.6	2	6434.5	0.0
64 5I 8	99.0	2	6444.2	0.0
65 5I 8	99.0	0	6444.8	0.0
66 5F 1	100.0	0	12241.3	0.0
67 5F 1	100.0	2	12317.9	0.0
68 5F 1	100.0	2	12346.4	0.0

TABLE VIII. ESTIMATED CRYSTAL FIELD PARAMETERS AND ENERGY LEVELS FOR  $\text{SmP}_{50}\text{O}_{14}$

SM IN  $\text{SmP}_{50}\text{O}_{14}$ . EXTERPOLATED BKM FROM COMPATIBLE ND AND EU HOMES. 9/24/75.

INIT. BKM AND CENTRICIDS. 0 = -0.000

-702.700 = B20	142.400 = B22	-146.700 = B40	363.800 = B42	635.900 = B42
224.100 = B60	323.900 = B62	176.400 = B62	229.200 = B64	-232.300 = B64
6H 5/2	134.0			
6H 7/2	1183.0	415.100 = B44	160.000 = B44	
6H 9/2	2398.0	-271.500 = B66	-208.900 = B66	
6H11/2	3737.0			
6H13/2	5098.0			
6F 1/2	6355.0			
6H15/2	6550.0			
6F 3/2	6700.0			
6F 5/2	7116.0			
6F 7/2	7995.0			
6F 9/2	9147.0			

FREE ION	PCT PURE	2MU	THEO. ENERGY	EXP. ENERGY
1 6H 5/2	98.6	1	-52.5	0.0
2 6H 5/2	98.6	1	136.7	0.0
3 6H 5/2	98.4	1	239.4	0.0
4 6H 7/2	98.6	1	1021.4	0.0
5 6H 7/2	98.1	1	1132.7	0.0
6 6H 7/2	97.4	1	1219.0	0.0
7 6H 7/2	98.5	1	1316.3	0.0
8 6H 9/2	98.6	1	2252.6	0.0
9 6H 9/2	98.2	1	2305.3	0.0
10 6H 9/2	98.4	1	2403.2	0.0
11 6H 9/2	98.2	1	2458.7	0.0
12 6H 9/2	98.9	1	2524.6	0.0
13 6H11/2	98.9	1	3566.7	0.0
14 6H11/2	98.1	1	3634.3	0.0
15 6H11/2	98.4	1	3713.8	0.0
16 6H11/2	98.2	1	3766.1	0.0
17 6H11/2	98.6	1	3820.0	0.0
18 6H11/2	98.7	1	3861.0	0.0
19 6H13/2	99.0	1	4882.3	0.0
20 6H13/2	98.3	1	4977.6	0.0
21 6H13/2	97.7	1	5075.7	0.0
22 6H13/2	98.4	1	5111.6	0.0
23 6H13/2	97.8	1	5159.5	0.0
24 6H13/2	98.6	1	5191.0	0.0
25 6H13/2	98.2	1	5224.5	0.0
26 6H15/2	98.4	1	6267.1	0.0
27 6F 1/2	95.5	1	6364.0	0.0
28 6H15/2	96.2	1	6383.3	0.0
29 6H15/2	98.2	1	6447.3	0.0
30 6H15/2	97.4	1	6516.8	0.0
31 6H15/2	97.8	1	6574.9	0.0
32 6H15/2	93.4	1	6664.5	0.0
33 6F 3/2	91.4	1	6699.8	0.0
34 6F 3/2	75.5	1	6726.1	0.0
35 6H15/2	89.5	1	6741.6	0.0
36 6H15/2	85.1	1	6790.2	0.0
37 6F 5/2	97.2	1	7114.2	0.0
38 6F 5/2	94.4	1	7153.8	0.0
39 6F 5/2	96.7	1	7166.9	0.0

TABLE VIII. ESTIMATED CRYSTAL FIELD PARAMETERS AND ENERGY LEVELS FOR  
SmP<sub>5</sub>O<sub>14</sub>

FREE ION	PCT PURE	2MU	THEO.ENERGY	EXP.ENERGY
40 6F 7/2	98.5	1	7967.4	0.C
41 6F 7/2	98.7	1	8009.0	0.C
42 6F 7/2	99.0	1	8026.5	0.C
43 6F 7/2	98.5	1	8063.8	0.C
44 6F 9/2	99.5	1	9107.9	0.C
45 6F 9/2	99.5	1	9134.2	0.C
46 6F 9/2	99.4	1	9179.4	0.C
47 6F 9/2	99.1	1	9194.1	0.C
48 6F 9/2	99.3	1	9219.2	0.C

TABLE IX. ENERGY LEVELS AND PHENOMENOLOGICAL  $B_{km}$  for  $\text{Eu}^{3+}$  IN  $\text{EuP}_{5014}$ <sup>a</sup>

EU IN P5014. NEW ASSIGNMENTS BASED ON SCALED BKM FROM ND HCF. 9/22/75.

FINAL BKM AND CENTROIDS.  $Q = 13.182$

-585.724 = B20    -212.651 = B22    -83.130 = B40    -751.307 = B42    -79.750 = B42  
131.526 = B60    117.952 = B62    -387.768 = B62    80.858 = B64    -67.600 = B64

7F 0	31.5				
7F 1	405.1	111.358 = B44	-183.577 = B44		
7F 2	1071.3	457.164 = B66	2.400 = B66		
7F 3	1935.4				
7F 4	2900.5				
7F 5	3919.3				
7F 6	5003.1				
FREE ION	PCT PURE	2MU	THEO. ENERGY	EXP. ENERGY	
1 7F 0	97.9	0	0.0	0.0	
2 7F 1	99.2	0	272.1	271.0	
3 7F 1	98.1	2	388.8	392.0	
4 7F 1	97.4	2	476.3	474.0	
5 7F 2	98.9	0	951.8	937.0*	
6 7F 2	97.0	2	971.3	960.0	
7 7F 2	97.5	2	1061.3	1070.0	
8 7F 2	95.0	0	1091.7	1097.0	
9 7F 2	95.8	0	1168.2	1180.0	
10 7F 3	98.5	2	1854.8	1869.0*	
11 7F 3	97.9	0	1886.2	1876.0	
12 7F 3	94.6	2	1902.1	1890.0	
13 7F 3	93.4	0	1911.9	1919.0	
14 7F 3	97.0	2	1960.6	1928.0*	
15 7F 3	94.7	0	1970.6	1982.0	
16 7F 3	97.6	2	1991.2	2012.0*	
17 7F 4	97.3	0	2742.2	2741.0	
18 7F 4	95.5	2	2783.9	2794.0	
19 7F 4	97.9	0	2833.6	2811.0*	
20 7F 4	95.9	2	2837.4	2844.0	
21 7F 4	96.5	0	2877.9	2869.0	
22 7F 4	95.4	0	2969.2	2973.0	
23 7F 4	97.4	2	2974.7	2979.0	
24 7F 4	97.8	2	3002.5	3007.0	
25 7F 4	97.8	0	3037.8	3040.0	
26 7F 5	98.7	2	3754.2	3748.0	
27 7F 5	98.1	2	3776.9	3774.0	
28 7F 5	96.6	0	3839.7	3864.0*	
29 7F 5	96.4	0	3900.7	3893.0	
30 7F 5	94.8	0	3911.8	3907.0	
31 7F 5	94.3	2	3919.3	3918.0	
32 7F 5	97.3	2	3946.5	3929.0*	
33 7F 5	98.5	2	3983.1	3984.0	
34 7F 5	96.3	0	4006.2	4018.0	
35 7F 5	97.4	0	4045.8	4049.0	
36 7F 5	97.9	2	4059.4	4061.0	
37 7F 6	99.2	0	4811.7	4798.0*	
38 7F 6	99.1	0	4812.7	4811.0	
39 7F 6	98.6	2	4907.4	4928.0*	
40 7F 6	98.4	2	4913.4	4952.0*	
41 7F 6	99.1	0	4966.4	4962.0	
42 7F 6	99.2	2	4972.2	4980.0	

<sup>a</sup>The least-rms deviation between the calculated and experimental energy levels is  $10.43 \text{ cm}^{-1}$  (C. Brecher, J. Chem. Phys., 61 (1974), 2297).



TABLE IX. ENERGY LEVELS AND PHENOMENOLOGICAL  $B_{km}$  FOR  $\text{Eu}^{3+}$  IN  $\text{EuP}_5\text{O}_{14}$ <sup>a</sup>  
(Cont'd)

FREE ION	PCI	PURE	2MU	THEO.ENERGY	EXP.ENERGY
43 7F 6		97.8	0	5024.2	4993.0*
44 7F 6		96.7	0	5047.6	5042.0
45 7F 6		97.0	2	5064.1	5057.0
46 7F 6		97.3	0	5145.6	5138.0
47 7F 6		97.5	2	5148.4	5160.0
48 7F 6		98.4	2	5266.6	5250.0*
49 7F 6		99.4	0	5266.9	5277.0

<sup>a</sup>The least-rms deviation between the calculated and experimental energy levels is  $10.43 \text{ cm}^{-1}$  (C. Brecher, J. Chem. Phys., 61 (1974), 2297).



TABLE X. ESTIMATED CRYSTAL FIELD PARAMETERS AND ENERGY LEVELS FOR  
EuP<sub>5</sub>O<sub>14</sub>

EU IN EUP<sub>5</sub>O<sub>14</sub>. EXTERPOLATED BKM FROM COMPATIBLE ND AND EU HOMES. 9/24/75.

INIT. BKM AND CENTRICIDS. Q = -0.000

-675.000 = B20 136.800 = B22 -140.400 = B40 696.100 = B42 81.700 = B42  
218.400 = B60 -114.300 = B62 340.900 = B62 245.000 = B64 -202.000 = B64

7F 0 96.0 238.100 = B44 -352.900 = B44  
7F 1 473.0 -330.400 = B66 -49.000 = B66  
7F 2 1175.0  
7F 3 1998.0  
7F 4 3000.0  
7F 5 4073.0  
7F 6 5094.0

5D 0 3 17220.0  
5D 1 3 18960.0  
5D 2 3 21422.0  
5D 3 3 24653.0

FREE ION PCT PURE 2MU THEO.ENERGY EXP.ENERGY

1 7F 0	97.6	0	61.1	0.0
2 7F 1	99.2	0	321.6	0.0
3 7F 1	97.6	2	478.7	0.0
4 7F 1	96.9	2	531.7	0.0
5 7F 2	96.7	2	1062.3	0.0
6 7F 2	98.1	0	1065.2	0.0
7 7F 2	96.9	2	1159.2	0.0
8 7F 2	93.5	0	1179.9	0.0
9 7F 2	95.9	0	1285.1	0.0
10 7F 3	98.2	2	1918.5	0.0
11 7F 3	97.3	0	1955.4	0.0
12 7F 3	95.1	2	1967.1	0.0
13 7F 3	92.2	0	1987.1	0.0
14 7F 3	96.8	2	2019.3	0.0
15 7F 3	94.3	0	2034.3	0.0
16 7F 3	96.7	2	2044.6	0.0
17 7F 4	97.4	0	2835.2	0.0
18 7F 4	95.3	2	2885.7	0.0
19 7F 4	97.4	0	2916.0	0.0
20 7F 4	95.7	2	2955.9	0.0
21 7F 4	96.2	0	3000.6	0.0
22 7F 4	96.2	0	3066.5	0.0
23 7F 4	97.5	2	3077.1	0.0
24 7F 4	97.7	2	3082.5	0.0
25 7F 4	97.5	0	3143.2	0.0
26 7F 5	98.4	2	3906.5	0.0
27 7F 5	97.9	2	3922.0	0.0
28 7F 5	94.9	0	4016.5	0.0
29 7F 5	96.6	0	4027.4	0.0
30 7F 5	93.2	2	4030.4	0.0
31 7F 5	94.5	0	4045.4	0.0
32 7F 5	97.9	2	4104.5	0.0
33 7F 5	97.7	2	4129.9	0.0
34 7F 5	96.5	0	4178.1	0.0
35 7F 5	97.5	0	4212.7	0.0
36 7F 5	98.3	2	4236.4	0.0
37 7F 6	99.2	0	4877.4	0.0
38 7F 6	99.0	0	4879.5	0.0
39 7F 6	98.2	2	4981.0	0.0
40 7F 6	98.0	2	4986.2	0.0
41 7F 6	98.2	0	5077.6	0.0
42 7F 6	98.2	2	5092.3	0.0
43 7F 6	96.3	0	5126.4	0.0

TABLE X. ESTIMATED CRYSTAL FIELD PARAMETERS AND ENERGY LEVELS FOR  
EuP<sub>5</sub>O<sub>14</sub> (Cont'd)

FREE ION	PCT PURE	2MU	THEO.ENERGY	EXP.ENERGY
44 7F 6		96.5 0	5156.7	0.0
45 7F 6		96.6 2	5190.9	0.0
46 7F 6		98.0 2	5244.8	0.0
47 7F 6		98.0 0	5249.4	0.0
48 7F 6		99.4 2	5349.1	0.0
49 7F 6		99.4 0	5349.2	0.0
50 5D 0	3	100.0 0	17219.4	0.0
51 5D 1	3	100.0 0	18920.9	0.0
52 5D 1	3	100.0 2	18968.9	0.0
53 5D 1	3	100.0 2	18988.6	0.0
54 5D 2	3	100.0 2	21401.2	0.0
55 5D 2	3	100.0 0	21404.2	0.0
56 5D 2	3	100.0 0	21418.5	0.0
57 5D 2	3	100.0 2	21439.8	0.0
58 5D 2	3	100.0 0	21445.2	0.0
59 5D 3	3	100.0 2	24618.2	0.0
60 5D 3	3	100.0 2	24629.1	0.0
61 5D 3	3	100.0 0	24651.3	0.0
62 5D 3	3	100.0 0	24651.9	0.0
63 5D 3	3	100.0 2	24655.4	0.0
64 5D 3	3	100.0 0	24683.7	0.0
65 5D 3	3	100.0 2	24684.9	0.0

TABLE XI. ESTIMATED CRYSTAL FIELD PARAMETERS AND ENERGY LEVELS FOR  
GdP<sub>5</sub>O<sub>14</sub>

5D IN GdP<sub>5</sub>O<sub>14</sub>. EXTERPOLATED BKM FROM COMPATIBLE ND AND EU HOMES. 9/24/75.

INIT. BKM AND CENTROIDS. Q = -0.000

-646.200 = B20    131.000 = B22    -133.700 = B40    456.700 = B42    -487.100 = B42  
212.700 = B60    -346.300 = B62    -51.700 = B62    257.700 = B64    -170.700 = B64

8S 7/2    0.0

6P 7/2    32210.3    -276.800 = B44    -296.500 = B44

6P 5/2    32753.0    -304.200 = B66    114.900 = B66

6P 3/2    33289.0

6I 7/2    35865.0

6I 9/2    36217.0

6I17/2    36448.0

6I11/2    36516.0

6I13/2    36700.0

6I15/2    36711.0

FREE ION    PCT PURE    2MU    THEO. ENERGY    EXP. ENERGY

1 8S 7/2    100.0    1    -0.4    0.0

2 8S 7/2    100.0    1    -0.2    0.0

3 8S 7/2    100.0    1    0.0    0.0

4 8S 7/2    100.0    1    0.3    0.0

5 6P 7/2    99.8    1    32137.7    0.0

6 6P 7/2    99.7    1    32177.6    0.0

7 6P 7/2    99.6    1    32213.5    0.0

8 6P 7/2    99.8    1    32272.0    0.0

9 6P 5/2    99.6    1    32713.0    0.0

10 6P 5/2    98.6    1    32733.9    0.0

11 6P 5/2    99.4    1    32777.5    0.0

12 6P 3/2    98.9    1    33261.1    0.0

13 6P 3/2    99.4    1    33299.3    0.0

14 6I 7/2    100.0    1    35842.9    0.0

15 6I 7/2    99.9    1    35863.6    0.0

16 6I 7/2    99.8    1    35877.7    0.0

17 6I 7/2    99.9    1    35886.9    0.0

18 6I 9/2    99.9    1    36188.9    0.0

19 6I 9/2    99.9    1    36205.0    0.0

20 6I 9/2    99.7    1    36225.4    0.0

21 6I 9/2    99.7    1    36231.3    0.0

22 6I 9/2    99.8    1    36245.3    0.0

23 6I17/2    98.6    1    36445.6    0.0

24 6I17/2    98.7    1    36445.7    0.0

25 6I17/2    99.3    1    36446.1    0.0

26 6I17/2    99.2    1    36446.2    0.0

27 6I17/2    99.0    1    36447.4    0.0

28 6I17/2    99.1    1    36448.3    0.0

29 6I17/2    98.2    1    36450.3    0.0

30 6I17/2    99.0    1    36453.5    0.0

31 6I17/2    99.1    1    36455.5    0.0

32 6I11/2    97.5    1    36485.5    0.0

33 6I11/2    97.9    1    36502.1    0.0

34 6I11/2    98.9    1    36511.1    0.0

35 6I11/2    98.6    1    36527.6    0.0

36 6I11/2    98.9    1    36535.8    0.0

37 6I11/2    98.9    1    36546.9    0.0

38 6I13/2    98.3    1    36666.0    0.0

39 6I13/2    98.6    1    36681.9    0.0

40 6I13/2    92.3    1    36686.4    0.0

41 6I13/2    92.0    1    36690.5    0.0

42 6I15/2    97.0    1    36693.6    0.0

43 6I15/2    92.6    1    36701.3    0.0

44 6I15/2    99.9    1    36706.8    0.0

TABLE XI. ESTIMATED CRYSTAL FIELD PARAMETERS AND ENERGY LEVELS FOR  
GdP<sub>5</sub>O<sub>14</sub> (Cont'd)

FREE ION	PCT PURE	2MU	THEO.ENERGY	EXP.ENERGY
45 6115/2	74.3	1	36710.6	0.C
46 6115/2	54.3	1	36713.1	0.C
47 6113/2	65.8	1	36717.5	0.C
48 6113/2	55.9	1	36723.0	0.C
49 6115/2	50.6	1	36726.3	0.C
50 6115/2	79.3	1	36731.2	0.C
51 6115/2	80.9	1	36741.8	0.C
52 6115/2	57.0	1	36743.5	0.C



TABLE XII. ESTIMATED CRYSTAL FIELD PARAMETERS AND ENERGY LEVELS FOR  
TbP<sub>5</sub>O<sub>14</sub>

TB IN TBPSC14. EXTERPOLATED BKM FROM COMPATIBLE ND AND EU HOMES. 9/24/75.

INIT. BKM AND CENTRICIDS. Q = -0.000

-616.000 = B20      124.900 = B22      -126.700 = B40      -114.000 = B42      -622.500 = B42  
206.700 = B60      -9.200 = B62      -340.200 = B62      266.500 = B64      -138.400 = B64

7F 6      310.0  
7F 5      2347.0  
7F 4      3580.0  
7F 3      4573.0  
7F 2      5155.0  
7F 1      5432.0  
7F 0      5766.0  
5D 4      3      20569.0  
5D 3      3      26357.0

FREE ION	PCT PURE	2MU	THEO. ENERGY	EXP. ENERGY
1 7F 6	99.6	2	88.8	0.0
2 7F 6	99.6	0	89.4	0.0
3 7F 6	99.3	0	170.7	0.0
4 7F 6	99.1	2	192.7	0.0
5 7F 6	99.3	2	215.9	0.0
6 7F 6	99.6	0	265.6	0.0
7 7F 6	99.8	2	289.1	0.0
8 7F 6	99.0	0	311.1	0.0
9 7F 6	99.3	0	313.4	0.0
10 7F 6	99.8	2	441.6	0.0
11 7F 6	99.8	2	447.8	0.0
12 7F 6	99.8	0	515.8	0.0
13 7F 6	99.8	0	518.4	0.0
14 7F 5	98.7	2	2196.0	0.0
15 7F 5	98.6	0	2213.3	0.0
16 7F 5	97.9	0	2249.5	0.0
17 7F 5	98.9	2	2294.8	0.0
18 7F 5	96.7	0	2298.9	0.0
19 7F 5	98.6	2	2322.9	0.0
20 7F 5	99.2	0	2381.1	0.0
21 7F 5	98.7	2	2387.9	0.0
22 7F 5	98.7	0	2444.4	0.0
23 7F 5	99.1	2	2465.0	0.0
24 7F 5	99.4	2	2489.1	0.0
25 7F 4	97.8	0	3404.3	0.0
26 7F 4	97.6	2	3495.5	0.0
27 7F 4	95.2	0	3543.6	0.0
28 7F 4	97.7	2	3547.1	0.0
29 7F 4	97.3	2	3595.3	0.0
30 7F 4	99.3	0	3603.7	0.0
31 7F 4	99.6	0	3648.4	0.0
32 7F 4	97.1	2	3658.3	0.0
33 7F 4	98.0	0	3720.2	0.0
34 7F 3	97.0	2	4522.0	0.0
35 7F 3	91.5	0	4528.0	0.0
36 7F 3	95.7	2	4547.8	0.0
37 7F 3	96.4	0	4578.2	0.0
38 7F 3	92.5	0	4592.2	0.0
39 7F 3	95.2	2	4593.5	0.0
40 7F 3	97.7	2	4647.0	0.0
41 7F 2	93.4	0	5067.6	0.0
42 7F 2	91.5	2	5137.1	0.0
43 7F 2	91.2	0	5177.6	0.0
44 7F 2	94.9	0	5217.1	0.0
45 7F 2	80.8	2	5250.1	0.0
46 7F 1	80.4	2	5393.4	0.0
47 7F 1	89.9	2	5451.8	0.0
48 7F 1	98.0	0	5579.1	0.0

TABLE XII. ESTIMATED CRYSTAL FIELD PARAMETERS AND ENERGY LEVELS FOR  
TbP<sub>5</sub>O<sub>14</sub> (Cont'd)

FREE ION	PCT PURE	2MU	THEO.ENERGY	EXP.ENERGY	
49 7F 0		94.0	0	5812.3	0.0
50 5D 4	3	100.0	0	20517.2	0.0
51 5D 4	3	100.0	2	20524.2	0.0
52 5D 4	3	100.0	0	20546.1	0.0
53 5D 4	3	100.0	2	20549.3	0.0
54 5D 4	3	100.0	0	20563.2	0.0
55 5D 4	3	100.0	2	20581.8	0.0
56 5D 4	3	100.0	2	20587.1	0.0
57 5D 4	3	100.0	0	20623.3	0.0
58 5D 4	3	100.0	0	20626.8	0.0
59 5D 3	3	100.0	2	26347.7	0.0
60 5D 3	3	100.0	0	26348.7	0.0
61 5D 3	3	100.0	0	26351.2	0.0
62 5D 3	3	100.0	2	26354.4	0.0
63 5D 3	3	100.0	2	26362.5	0.0
64 5D 3	3	100.0	2	26368.4	0.0
65 5D 3	3	100.0	0	26368.6	0.0

TABLE XIII. ESTIMATED CRYSTAL FIELD PARAMETERS AND ENERGY LEVELS FOR  
DyP<sub>5</sub>O<sub>14</sub>

DY IN DYP5O14. EXTERPOLATED BKM FROM COMPATIBLE ND AND EU HOMES. 9/24/75.

INIT. BKM AND CENTRICIDS. Q = -0.000

-584.300 = B20      118.500 = B22      -119.300 = B40      -535.200 = B42      -262.000 = B42  
200.600 = B60      323.500 = B62      -66.400 = B62      271.300 = B64      -107.000 = B64

6H15/2      262.0  
6H13/2      3710.0      106.800 = B44      345.700 = B44  
6H11/2      6028.0      -58.800 = B66      301.100 = B66  
6F11/2      7830.0  
6H 9/2      7879.0  
6F 9/2      9188.0  
6H 7/2      9243.0  
6H 5/2      10340.0  
6F 7/2      11071.0  
6F 5/2      12462.0

FREE ION	PCT PURE	2MU	THEO. ENERGY	EXP. ENERGY
1 6H15/2	100.0	1	32.7	0.0
2 6H15/2	99.9	1	137.8	0.0
3 6H15/2	99.9	1	178.0	0.0
4 6H15/2	99.9	1	230.2	0.0
5 6H15/2	99.9	1	262.2	0.0
6 6H15/2	99.9	1	311.5	0.0
7 6H15/2	99.9	1	378.4	0.0
8 6H15/2	99.9	1	508.0	0.0
9 6H13/2	99.9	1	3554.6	0.0
10 6H13/2	99.7	1	3622.6	0.0
11 6H13/2	99.6	1	3672.3	0.0
12 6H13/2	99.8	1	3686.2	0.0
13 6H13/2	99.8	1	3725.9	0.0
14 6H13/2	99.6	1	3798.0	0.0
15 6H13/2	99.7	1	3861.9	0.0
16 6H11/2	99.4	1	5423.2	0.0
17 6H11/2	99.2	1	5453.9	0.0
18 6H11/2	99.2	1	5971.9	0.0
19 6H11/2	99.4	1	6015.8	0.0
20 6H11/2	99.2	1	6093.6	0.0
21 6H11/2	99.5	1	6156.8	0.0
22 6F11/2	59.4	1	7704.5	0.0
23 6F11/2	49.7	1	7734.5	0.0
24 6F11/2	56.7	1	7767.0	0.0
25 6F11/2	52.8	1	7783.4	0.0
26 6F11/2	78.2	1	7810.5	0.0
27 6F11/2	73.1	1	7833.0	0.0
28 6F11/2	67.6	1	7872.3	0.0
29 6H 9/2	64.4	1	7900.9	0.0
30 6F11/2	65.1	1	7944.7	0.0
31 6H 9/2	70.7	1	7977.5	0.0
32 6H 9/2	66.7	1	8047.3	0.0
33 6F 9/2	53.6	1	9058.6	0.0
34 6H 7/2	58.9	1	9107.7	0.0
35 6F 9/2	62.3	1	9144.5	0.0
36 6F 9/2	87.3	1	9182.5	0.0
37 6F 9/2	87.9	1	9211.1	0.0
38 6F 9/2	78.8	1	9235.3	0.0
39 6H 7/2	63.5	1	9281.6	0.0
40 6H 7/2	61.9	1	9328.0	0.0
41 6H 7/2	83.9	1	9392.1	0.0

TABLE XIII. ESTIMATED CRYSTAL FIELD PARAMETERS AND ENERGY LEVELS FOR  
DyP<sub>5</sub>O<sub>14</sub> (Cont'd)

FREE ION	PCT PURE	2MU	THEO.ENERGY	EXP.ENERGY
42 6H 5/2	96.9	1	10228.6	0.C
43 6H 5/2	97.7	1	10332.4	0.C
44 6H 5/2	95.3	1	10464.7	0.C
45 6F 7/2	97.6	1	11057.1	0.0
46 6F 7/2	99.1	1	11085.1	0.C
47 6F 7/2	97.5	1	11102.0	0.0
48 6F 7/2	98.7	1	11122.1	0.C
49 6F 5/2	99.6	1	12447.9	0.C
50 6F 5/2	99.8	1	12482.5	0.C
51 6F 5/2	99.6	1	12495.9	0.C



TABLE XIV. ESTIMATED CRYSTAL FIELD PARAMETERS AND ENERGY LEVELS FOR  
HoP<sub>5</sub>O<sub>14</sub>

HO IN HOP5O14. EXTERPOLATED BKM FROM COMPATIBLE ND AND EU HOMES. 5/24/75.

INIT. BKM AND CENTRICIS. Q = -0.000

-550.800 = B20    111.700 = B22    -111.400 = B40    -493.800 = B42    256.500 = B42  
194.300 = B60    117.900 = B62    297.400 = B62    272.200 = B64    -75.500 = B64

51 8    169.6  
51 7    5219.5    337.000 = B44    -25.000 = B44  
51 6    8717.6    92.300 = B66    282.500 = B66  
51 5    11274.7  
51 4    13333.4

FREE ION	PCT PURE	2MU	THEO. ENERGY	EXP. ENERGY
1 51 8	100.0	0	17.0	0.0
2 51 8	100.0	2	18.9	0.0
3 51 8	100.0	2	31.4	0.0
4 51 8	100.0	0	40.7	0.0
5 51 8	100.0	0	69.1	0.0
6 51 8	100.0	2	102.6	0.0
7 51 8	100.0	0	138.4	0.0
8 51 8	100.0	2	167.3	0.0
9 51 8	100.0	0	170.2	0.0
10 51 8	100.0	2	201.6	0.0
11 51 8	100.0	0	226.8	0.0
12 51 8	100.0	0	246.9	0.0
13 51 8	100.0	2	247.3	0.0
14 51 8	100.0	2	275.8	0.0
15 51 8	100.0	2	286.3	0.0
16 51 8	100.0	0	303.3	0.0
17 51 8	100.0	0	306.6	0.0
18 51 7	100.0	0	5138.6	0.0
19 51 7	100.0	2	5138.7	0.0
20 51 7	100.0	2	5183.1	0.0
21 51 7	99.9	0	5183.3	0.0
22 51 7	99.9	2	5197.2	0.0
23 51 7	99.9	0	5197.7	0.0
24 51 7	99.9	2	5205.0	0.0
25 51 7	100.0	0	5205.0	0.0
26 51 7	99.9	2	5224.3	0.0
27 51 7	99.9	0	5232.5	0.0
28 51 7	99.9	2	5240.4	0.0
29 51 7	99.9	0	5264.2	0.0
30 51 7	99.9	0	5269.7	0.0
31 51 7	99.9	2	5296.3	0.0
32 51 7	100.0	2	5296.4	0.0
33 51 6	99.9	2	8639.8	0.0
34 51 6	99.9	0	8640.7	0.0
35 51 6	99.9	0	8689.3	0.0
36 51 6	99.9	2	8692.5	0.0
37 51 6	99.9	2	8705.5	0.0
38 51 6	99.9	0	8704.3	0.0
39 51 6	99.8	0	8715.4	0.0
40 51 6	99.8	2	8720.4	0.0
41 51 6	99.9	0	8735.0	0.0
42 51 6	99.8	2	8745.9	0.0
43 51 6	99.8	2	8751.4	0.0
44 51 6	99.9	0	8784.5	0.0
45 51 6	99.9	0	8790.0	0.0
46 51 5	99.7	0	11204.3	0.0
47 51 5	99.9	2	11211.4	0.0
48 51 5	99.8	0	11254.2	0.0
49 51 5	99.6	2	11256.7	0.0
50 51 5	99.8	2	11265.3	0.0
51 51 5	99.7	0	11269.2	0.0
52 51 5	99.7	2	11285.4	0.0
53 51 5	99.5	0	11288.4	0.0
54 51 5	99.8	0	11305.7	0.0

TABLE XIV. ESTIMATED CRYSTAL FIELD PARAMETERS AND ENERGY LEVELS FOR  
HoP<sub>5</sub>O<sub>14</sub> (Cont'd)

FREE ION	PCT PURE	2Mμ	THEO.ENERGY	EXP.ENERGY
55 51 5	99.5	2	11332.2	0.C
56 51 5	99.3	2	11341.1	0.C
57 51 4	99.8	0	13244.2	0.C
58 51 4	99.7	2	13244.6	0.C
59 51 4	99.8	0	13285.0	0.C
60 51 4	99.3	0	13298.7	0.C
61 51 4	99.5	2	13328.1	0.C
62 51 4	99.8	2	13336.7	0.C
63 51 4	99.9	2	13426.9	0.C
64 51 4	99.8	0	13427.6	0.C
65 51 4	100.0	0	13462.8	0.C

TABLE XV. ESTIMATED CRYSTAL FIELD PARAMETERS AND ENERGY LEVELS FOR  $\text{ErP}_5\text{O}_{14}$

ER IN  $\text{ErP}_5\text{O}_{14}$ . EXTERPOLATED BKM FROM COMPATIBLE ND AND EU HOMES. 9/24/75.

INIT. BKM AND CENTRICIDS.  $Q = -0.000$

-515.000 = B20    104.400 = B22    -102.900 = B40    -80.600 = B42    507.700 = B42  
187.800 = B60    -263.100 = B62    162.300 = B62    269.300 = B64    -45.200 = B64

4I15/2    263.0  
4I13/2    6736.0    47.200 = B44    -308.500 = B44  
4I11/2    10346.0    210.800 = B66    195.100 = B66  
4I 9/2    12560.0  
4F 9/2    15365.0  
4S 3/2    18444.0  
2H11/2 2    19190.0  
4F 7/2    20582.0  
4F 5/2    22230.0  
4F 3/2    22561.0

FREE ION	PCT PURE	2MU	THEO. ENERGY	EXP. ENERGY
1 4I15/2	100.0	1	87.5	0.0
2 4I15/2	100.0	1	119.0	0.0
3 4I15/2	100.0	1	199.3	0.0
4 4I15/2	100.0	1	251.7	0.0
5 4I15/2	100.0	1	306.1	0.0
6 4I15/2	100.0	1	337.9	0.0
7 4I15/2	100.0	1	369.6	0.0
8 4I15/2	100.0	1	413.5	0.0
9 4I13/2	100.0	1	6632.6	0.0
10 4I13/2	99.9	1	6668.6	0.0
11 4I13/2	99.9	1	6717.9	0.0
12 4I13/2	99.9	1	6733.3	0.0
13 4I13/2	100.0	1	6782.0	0.0
14 4I13/2	100.0	1	6795.0	0.0
15 4I13/2	100.0	1	6808.2	0.0
16 4I11/2	99.9	1	10289.2	0.0
17 4I11/2	99.9	1	10316.4	0.0
18 4I11/2	99.9	1	10340.7	0.0
19 4I11/2	99.9	1	10363.9	0.0
20 4I11/2	99.9	1	10372.1	0.0
21 4I11/2	100.0	1	10389.6	0.0
22 4I 9/2	99.9	1	12458.6	0.0
23 4I 9/2	99.9	1	12477.0	0.0
24 4I 9/2	100.0	1	12585.7	0.0
25 4I 9/2	100.0	1	12612.5	0.0
26 4I 9/2	100.0	1	12661.7	0.0
27 4F 9/2	99.9	1	15289.2	0.0
28 4F 9/2	100.0	1	15344.6	0.0
29 4F 9/2	100.0	1	15362.0	0.0
30 4F 9/2	99.9	1	15407.1	0.0
31 4F 9/2	99.9	1	15428.3	0.0
32 4S 3/2	99.3	1	18409.0	0.0
33 4S 3/2	98.9	1	18468.4	0.0
34 2H11/2 2	99.7	1	19144.8	0.0
35 2H11/2 2	99.3	1	19164.0	0.0
36 2H11/2 2	99.7	1	19168.3	0.0
37 2H11/2 2	99.6	1	19192.9	0.0
38 2H11/2 2	99.2	1	19223.8	0.0
39 2H11/2 2	99.5	1	19250.2	0.0
40 4F 7/2	99.8	1	20515.6	0.0
41 4F 7/2	99.5	1	20563.8	0.0
42 4F 7/2	99.5	1	20598.1	0.0
43 4F 7/2	99.7	1	20665.4	0.0

TABLE XV. ESTIMATED CRYSTAL FIELD PARAMETERS AND ENERGY LEVELS FOR  
 $\text{ErP}_5\text{O}_{14}$  (Cont'd)

FREE ION	PCT PURE	2MU	THEO.ENERGY	EXP.ENERGY
44 4F 5/2	99.5	1	22210.3	0.C
45 4F 5/2	97.6	1	22222.8	0.C
46 4F 5/2	99.4	1	22258.9	0.C
47 4F 3/2	98.1	1	22527.0	0.C
48 4F 3/2	97.7	1	22615.0	0.C



TABLE XVI. ESTIMATED CRYSTAL FIELD PARAMETERS AND ENERGY LEVELS FOR  
 $\text{TmP}_5\text{O}_{14}$

TM IN  $\text{TMPO}_{14}$ . EXTERPOLATED BKM FROM COMPATIBLE ND AND EU HOMES. 3/24/75.

INIT. BKM AND CENTRICIDS. C = -0.000

-476.600 = B20      96.600 = B22      -93.700 = B40      328.000 = B42      333.600 = B42  
 181.100 = B60      -198.300 = B62      -222.500 = B62      262.700 = B64      -16.200 = B64

3H 6      255.0  
 3F 4      5820.0      -264.000 = B44      -104.700 = B44  
 3H 5      8435.0      264.100 = B66      65.300 = B66  
 3H 4      12731.0

3F 3      14529.0

3F 2      15133.0

1G 4      21325.0

1D 2      27892.0

FREE ION      PCT PURE      2MU      THFO.ENERGY      EXP.ENERGY

1 3H 6      100.0      0      -1.3      0.0

2 3H 6      100.0      0      9.3      0.0

3 3H 6      100.0      2      143.9      0.0

4 3H 6      100.0      2      170.7      0.0

5 3H 6      100.0      0      242.2      0.0

6 3H 6      100.0      2      252.7      0.0

7 3H 6      100.0      0      285.7      0.0

8 3H 6      100.0      0      319.0      0.0

9 3H 6      100.0      2      330.7      0.0

10 3H 6      100.0      2      346.9      0.0

11 3H 6      100.0      0      351.8      0.0

12 3H 6      99.9      2      408.4      0.0

13 3H 6      99.9      0      410.3      0.0

14 3F 4      99.8      2      5691.8      0.0

15 3F 4      99.6      0      5712.5      0.0

16 3F 4      99.8      0      5779.7      0.0

17 3F 4      99.7      2      5787.3      0.0

18 3F 4      99.9      0      5827.5      0.0

19 3F 4      99.9      2      5842.5      0.0

20 3F 4      100.0      0      5874.3      0.0

21 3F 4      99.9      0      5917.5      0.0

22 3F 4      99.9      2      5927.4      0.0

23 3H 5      100.0      2      8243.8      0.0

24 3H 5      99.8      2      8251.2      0.0

25 3H 5      99.7      0      8375.5      0.0

26 3H 5      99.9      0      8379.6      0.0

27 3H 5      99.9      2      8451.2      0.0

28 3H 5      99.9      0      8471.6      0.0

29 3H 5      99.9      2      8474.8      0.0

30 3H 5      99.8      0      8513.7      0.0

31 3H 5      99.9      2      8514.0      0.0

32 3H 5      99.8      2      8554.2      0.0

33 3H 5      99.9      0      8556.3      0.0

34 3H 4      99.6      0      12547.4      0.0

35 3H 4      100.0      0      12610.5      0.0

36 3H 4      99.6      2      12671.9      0.0

37 3H 4      99.6      0      12751.2      0.0

38 3H 4      99.8      2      12757.8      0.0

39 3H 4      99.8      2      12765.2      0.0

40 3H 4      99.8      0      12792.7      0.0

41 3H 4      99.6      2      12815.1      0.0

42 3H 4      99.6      0      12830.0      0.0

43 3F 3      99.3      0      14490.8      0.0

44 3F 3      99.6      2      14494.9      0.0

45 3F 3      99.3      0      14515.1      0.0

46 3F 3      99.7      2      14534.1      0.0

47 3F 3      99.3      0      14553.7      0.0

48 3F 3      99.7      2      14559.2      0.0

49 3F 3      99.5      2      14592.6      0.0

TABLE XVI. ESTIMATED CRYSTAL FIELD PARAMETERS AND ENERGY LEVELS FOR  
 $\text{TmP}_5\text{O}_{14}$  (Cont'd)

FREE ION	PCT PURE	2MU	THEO.ENERGY	EXP.ENERGY
50 3F 2	99.2	0	15083.4	0.C
51 3F 2	99.6	2	15085.9	0.C
52 3F 2	99.2	2	15133.7	0.C
53 3F 2	99.6	0	15176.8	0.C
54 3F 2	99.8	0	15225.3	0.C
55 1G 4	100.0	2	21160.6	0.C
56 1G 4	100.0	0	21167.9	0.C
57 1G 4	100.0	0	21252.7	0.C
58 1G 4	100.0	2	21312.3	0.C
59 1G 4	100.0	0	21313.9	0.C
60 1G 4	100.0	2	21344.2	0.C
61 1G 4	100.0	0	21385.8	0.C
62 1G 4	100.0	0	21484.9	0.C
63 1G 4	100.0	2	21511.7	0.C
64 1D 2	100.0	0	27822.8	0.C
65 1D 2	100.0	2	27837.9	0.C
66 1D 2	100.0	2	27885.6	0.C
67 1D 2	100.0	0	27957.9	0.C
68 1D 2	100.0	0	27970.5	0.C

TABLE XVII. AMPLITUDES,  $A_{km}$ , IN  $\text{CM}^{-1} \text{\AA}^{-k}$ , OF SPHERICAL DECOMPOSITION OF LATTICE SUMS FOR  $\text{NdP}_5\text{O}_{14}^{\dagger}$

k	m	$A_{km} (q_0 = -1)^{\ddagger}$		$A_{km} (q_0 = -2)^{\ddagger}$	
		Real	Imaginary	Real	Imaginary
1	0	16797.4	0	23799.2	0
1	1	-37138.	5876.2	-69989.6	12348.9
2	0	-3006.66	0	-5414.44	0
2	1	24.0762	-210.429	32.735	-440.936
2	2	-46.2236	-699.385	-476.544	-742.301
3	0	146.631	0	272.599	0
3	1	113.903	-113.566	245.472	174.387
3	2	23.9621	118.058	23.3478	221.346
3	3	-107.	206.525	-512.996	235.769
4	0	1459.8	0	2659.56	0
4	1	-104.684	-153.643	-210.048	-308.525
4	2	-1196.65	985.944	-2418.41	1926.86
4	3	194.779	9.65227	400.361	21.1591
4	4	-658.119	-1337.65	-1156.92	-2600.78
5	0	-4.45292	0	-8.32774	0
5	1	759.959	-413.245	1502.53	-818.815
5	2	-33.9232	-12.0518	-69.3783	-25.2627
5	3	55.5247	-1357.2	124.874	-2646.4
5	4	74.1133	-34.314	148.632	-68.9808
5	5	-267.703	-218.441	-554.059	-448.519
6	0	202.617	0	403.34	0
6	1	2.44617	23.9365	5.33098	48.019
6	2	-95.8561	130.302	-189.637	258.726
6	3	-11.6831	-17.1279	-22.8872	-34.8373
6	4	-52.1825	-134.274	-116.977	-267.059
6	5	-12.6303	10.3804	-25.5546	20.0073
6	6	206.515	22.0685	411.215	43.7949
7	0	4.1059	0	8.26562	0
7	1	-47.8198	51.1209	-94.1572	101.206
7	2	-5.24923	-7.26414	-10.3708	-14.4391
7	3	-3.467	-15.118	-6.88997	-30.8619
7	4	4.838	1.1332	9.7122	2.29936
7	5	-25.74	-28.179	-51.1031	-56.7309
7	6	1.327	10.5704	2.61491	21.295
7	7	-32.06	20.2109	-64.6403	39.2683

<sup>†</sup>Lattice constants are  $a = 8.771 \text{ \AA}$ ,  $b = 9.012 \text{ \AA}$ ,  $c = 13.057 \text{ \AA}$ , and  $\beta = 89.58 \text{ deg}$  (H. Y-P. Hong, *Acta Crystallogr.*, B30 (1974), 468).

<sup>‡</sup>Oxygen charge,  $q_0$ . Neodymium and phosphorus charges taken as  $q_{\text{Nd}} = +3$ ,  $q_{\text{P}} = -(3 + 14q_0)/5$ .

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